

Lifting of the Landau level degeneracy in graphene devices in a tilted magnetic field

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We report on transport and capacitance measurements of graphene devices in magnetic fields up to 30 T. In both techniques, we observe the full splitting of Landau levels and we employ tilted field experiments to address the origin of the observed broken symmetry states. In the lowest energy level, the spin degeneracy is removed at filling factors $\nu = \pm 1$ and we observe an enhanced energy gap. In the higher levels, the valley degeneracy is removed at odd filling factors while spin polarized states are formed at even ν . Although the observation of odd filling factors in the higher levels points towards the spontaneous origin of the splitting, we find that the main contribution to the gap at $\nu = -4, -8$, and -12 is due to the Zeeman energy.

One of the prominent consequences of the Dirac-like nature of charge carriers in graphene is the half-integer quantum Hall effect. The Hall conductance is quantized to half-integer multiples of $4e^2/h$, reflecting the spin and valley degeneracy of the Landau levels (LLs) at filling factors $\nu = 4(N + 1/2) = \pm 2, \pm 6, \pm 10, \dots$ [1, 2], where N is the LL index.

However, electron-electron interactions and explicit symmetry breaking fields, such as the Zeeman splitting, can lift the LL degeneracy, leading to the observation of the integer quantum Hall effect in intermediate states. The origin and the possible spin and/or valley polarization of the broken symmetry states has been the subject of considerable theoretical interest [3–9] and experimental investigations [10–17].

Earlier experimental works on graphene on SiO₂ reported the partial splitting of $N = \pm 1$ at $\nu = \pm 4$ [10, 11, 16] as a single particle effect due to the Zeeman energy, and the full splitting in the lowest LL driven by electron-electron interactions [11]. Experiments on cleaner devices deposited on hexagonal boron nitride (hBN) showed the full sequence of integer filling factors and addressed the role of electron-electron interactions in the LLs splitting [15, 18], revealing enhanced gaps in the higher LLs and skyrmion mediated transport in $N = -1$ [15]. These observations have been attributed to the quantum Hall ferromagnetism (QHF) in graphene [19].

In this Rapid Communication we report on the LL splitting in graphene encapsulated between two layers of h-BN and we investigate the nature of the states occurring at integer ν due to the lifting of the LL degeneracy. Thermally activated transport in both perpendicular and tilted magnetic fields up to 30 T, supported qualitatively by capacitance spectroscopy [20], enables us to probe the origin of the states at $\nu = -1, -3, -4, -7, -8, -12$. We show that in the lowest LL, a spin unpolarized state is formed at $\nu = 0$ and the spin degeneracy is removed at $\nu = \pm 1$. In the higher levels, the even ν separate two fully spin polarized states while the odd ν originate from the lifting of the valley degeneracy, supporting the findings of Ref. 15. We find that, for $|N| \geq 1$, the gap at half

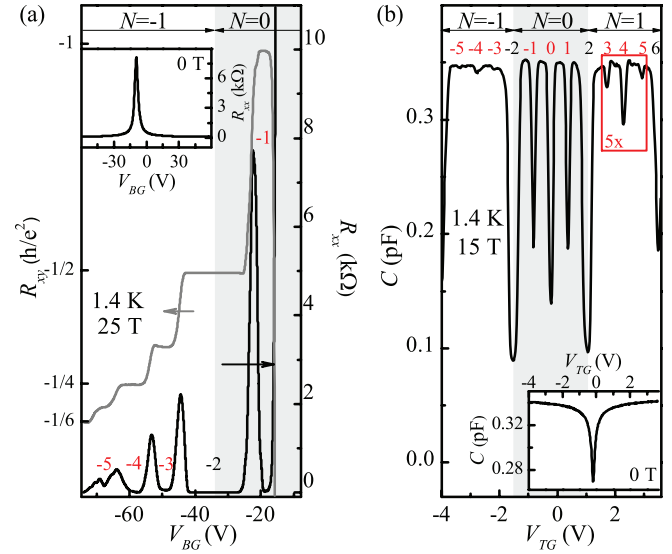


FIG. 1. (Color online) Transport and capacitance measurements at 1.4 K. (a) R_{xx} (black line) and R_{xy} (gray line) as a function of the back gate voltage V_{BG} at 25 T. Inset: R_{xx} as a function of V_{BG} at 0 T. (b) C as a function of the top gate voltage V_{TG} at 15 T. The curve inside the red box is expanded five times and shifted in order to match the constant background of the original curve. The numbers close to the minima of R_{xx} and C indicate the filling factors. Inset: C as a function of V_{TG} at 0 T.

filling is set by the Zeeman energy and we demonstrate that the interactions, although relevant in determining the splitting of the higher levels, are not the dominant energy scale for $|N| > 0$ in our devices.

We focus on two single layer graphene devices. In both devices the graphene flake is sandwiched between two h-BN flakes. Device A is a Hall bar ($W \approx 1.3 \mu\text{m}$, $L/W = 2$) for standard magneto-transport measurements. The longitudinal (R_{xx}) and Hall (R_{xy}) resistances are measured as a function of the back gate voltage (V_{BG}) using a low noise lock-in technique with a 10 nA excitation current at 13 Hz. Measurements at the charge neutrality point (CNP) in a magnetic field are performed in

a constant voltage configuration with a 100 μV excitation. Device B is a graphene-hBN-Au capacitor, similar to the ones described in Ref. 18, with a 37 nm thick h-BN flake between the graphene and the Au electrode. The capacitance C is measured as a function of the DC voltage (V_{TG}) applied between the top gate and the graphene sheet using a capacitance bridge (AH2700) with 30 mV AC excitation at 20 kHz. C embodies two major contributions: the geometrical capacitance $C_G = 0.346$ pF and the quantum capacitance C_Q , which is directly proportional to the density of states (DOS) [21] of graphene. Both devices were placed in a variable temperature ^4He cryostat in a Bitter magnet on a sample holder which allows *in situ* rotation.

We first characterize our devices at $T=1.4$ K in the absence of a magnetic field. As illustrated in the insets of Figs. 1(a) and 1(b) both samples are n -doped and the CNP is situated at $V_{BG}^{CNP} \approx -10$ V for device A and $V_{TG}^{CNP} \approx -0.2$ V for device B, corresponding to a residual electron concentration $n_A \approx 6 \times 10^{11} \text{ cm}^{-2}$ and $n_B \approx 1 \times 10^{11} \text{ cm}^{-2}$, respectively. The field effect mobility has been extracted for device A according to Ref. 22 and is found to be $\mu = 4 \cdot 10^4 \text{ cm}^2/\text{Vs}$.

In a magnetic field, both samples show the full lifting of the Landau level degeneracy. In Fig. 1(a) we show R_{xx} of device A at 25 T and 1.4 K for the hole side ($V_{BG} < V_{BG}^{CNP}$). Minima in R_{xx} and quantized Hall plateaus in R_{xy} at $\nu = -1, -3, -4$, and -5 are well developed and more pronounced compared to those observed in the electron side. We will therefore focus our further analysis on the LLs for the holes. For device B [Fig. 1(b)], clear minima in the capacitance measurements are detected at each integer value of ν in $N = 0$ and $N = \pm 1$ at 15 T and 1.4 K. It is worth noting that the lifting of the LL degeneracy evolves progressively with the magnetic field, first in the lowest LL and then in the higher levels and, within each level, first at half filling and then at quarter filling. Hence, the first filling factor observed is $\nu = 0$, appearing as a clear minimum in C for $B \geq 5$ T and as a diverging R_{xx} for $B > 2$ T [see Fig. 4(c), points connected by the grey line]. Filling factors $\nu = \pm 1$ are well developed already at 10 T for both samples. For $B \geq 10$ T the full splitting of $N = \pm 1$ starts to be resolved in the capacitance spectroscopy. In transport measurements, plateaus in R_{xy} appear in the $N = -1$ LL, first at $\nu = -4$ (10 T), then at $\nu = -3$ (12.5 T), and finally at $\nu = -5$ (17.5 T).

Let us now address the sizes of the energy gaps Δ_ν that are associated with the broken symmetry states in a purely perpendicular magnetic field (Fig. 2). We extract Δ_ν from temperature-activated transport experiments on device A between 1.4 and 18 K, fitting the experimental data according to the Fermi-Dirac distribution $R_{xx} \propto 1/(e^{-\Delta_\nu/2k_B T} + 1)$, since the size of the gap is comparable to $k_B T$ in the temperature range under study [23]. The inset of Fig. 2 shows the minima

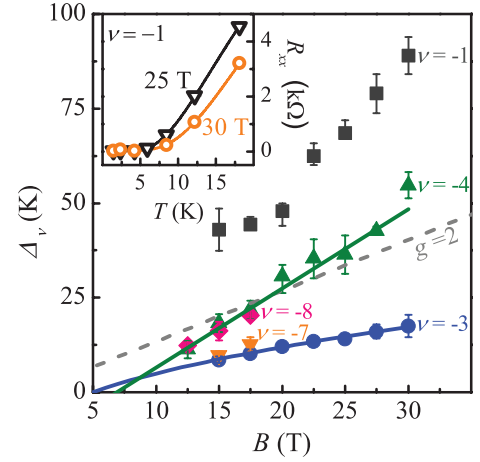


FIG. 2. (Color online) Activation gaps Δ_ν as a function of B for $\nu = -1, -3, -4, -7$ and -8 . The gray dashed line indicates E_Z calculated with $g = 2$, and the solid lines are the linear (green) and square root (blue) fit to the data. Inset: R_{xx} minima of $\nu = -1$ as a function of temperature at 25 T (black triangles) and 30 T (orange circles), and the solid lines are a fit to the experimental data according to the Fermi-Dirac distribution. The relatively large error bars for gaps exceeding 20 K are due to the fact that the temperature range used (1.4 – 18 K) was not large enough to access them more accurately.

of R_{xx} as a function of temperature for $\nu = -1$ at 25 (triangles) and 30 T (circles) and the fits (solid lines) as an example of typical fitting traces. Since there is some uncertainty in the range of applicability of the activated transport assumption, at some magnetic field values we had to perform different fits considering each time a different temperature range. The values of Δ_ν plotted in Fig. 2 are an average over the values obtained fitting in the different temperature ranges, and the error bars represent the spread of all the values obtained due to the different fits.

As can be seen in Fig. 2, the size of the energy gaps increases with the magnetic field for each filling factor. In the higher LLs ($N = -1$ and -2) we can distinguish between two different energy scales, one for the gaps at even ν and one for the gaps at odd ν . The size of Δ_{-4} and Δ_{-8} increases linearly with the magnetic field and the gaps for both filling factors fall on the same line. The gap size can be described by $\Delta = g\mu_B B - \Gamma$; the first term is the Zeeman energy (E_Z) and Γ is the Landau level broadening. A fit to the experimental data yields $g = 3.1 \pm 0.1$ and $\Gamma = 14.4 \pm 1.5$ K. The enhancement of g compared to its bare value 2 is probably due to exchange interaction [24].

The gaps at odd filling factors within the $N = -1$ and $N = -2$ LLs, Δ_{-3} and Δ_{-7} , are comparable within the error bars. They are considerably smaller than E_Z and their field dependence can be fitted by a square root function with a finite offset representing a Landau level

broadening of 12 ± 1 K (blue solid line for of Δ_{-3}). A linear function, which would also reasonably fit the data, leads to a meaningless negative value for Γ .

Though a shallow minimum develops in R_{xx} at $\nu = -5$ for $B > 17.5$ T, we are not able to extract the activated gap in the considered temperature range since the R_{xx} minimum is visible only at the lowest temperatures. Thus, we conclude that the state at $\nu = -5$ is weaker than the state at $\nu = -3$, as also suggested by the capacitance signal where dips at $\nu = \pm 5$ are not as pronounced as the ones at $\nu = \pm 3$ [see the curve inside the red box in Fig. 1(b)].

In addition, Fig. 2 highlights already the different behavior of the states within the lowest LL compared to the ones in the higher levels. Indeed we notice that $\nu = -1$ has the largest energy gap and, in particular, it is much larger than the size of the gaps of the other odd filling factor $\nu = -3$ and $\nu = -7$.

In order to further investigate the origin of the broken symmetry states we perform magnetotransport and capacitance experiments in a tilted magnetic field. We tilt the sample with respect to the direction of the magnetic field by an angle θ [see inset of Fig. 3(a)], while keeping constant the component of the magnetic field perpendicular to the graphene plane (B_{\perp}), thus increasing the total magnetic field (B_T) applied to the sample. The effects related to the spin can be decoupled from those dependent on B_{\perp} alone. For device A, the experiments in a tilted magnetic field were performed in two different cooldowns, indicated by solid symbols (first cooldown) and open symbols (second cooldown) in Figs. 3 and 4.

In Fig. 3, we illustrate the splitting of the higher LLs ($N > 0$) for different tilt angles. The minima in R_{xx} and C associated with even ν become more pronounced upon tilting the sample and increasing B_T , while those associated with the odd filling factors do not change. In particular, for $B_{\perp} = 8.4$ T and $\theta = 0^\circ$, we observe only the standard sequence for the half-integer quantum Hall effect in graphene [Fig. 3(a) black line] while at $\theta = 73.7^\circ$ clear minima in R_{xx} appear at the intermediate filling factors $\nu = -4, -8$, and -12 (red line). In the capacitance signal shown in Fig. 3(c), the minimum at $\nu = 4$ becomes progressively deeper as the sample is tilted from 0° to 63.2° , indicating that the DOS is reduced by an increase in B_T . In contrast, the minima at $\nu = -3$ and -7 in R_{xx} [Fig. 3(b)] and $\nu = 3$ and 5 in C [Fig. 3(c)] do not show any significant change as the sample is tilted.

We address quantitatively the splitting mechanism for the higher energy LLs extracting the activation gaps in a tilted magnetic field. As Fig. 3(d) shows, Δ_{-4} , Δ_{-8} , and Δ_{-12} increase linearly with B_T at a fixed $B_{\perp} = 10.4$ T and the gap size is smaller than the Zeeman energy (gray dashed line). The linear dependence of Δ_{-4} and Δ_{-8} on B_T is found at several B_{\perp} (10.4, 11.3, 20, and 25 T, the last two only for Δ_{-4}). At even ν , the gap size can be described as a result of two separate

contributions reduced by the Landau level broadening, $\Delta_{\nu} = E(B_{\perp}) + E_Z(B_T) - \Gamma$. The first term, $E(B_{\perp})$, incorporates all the effects which depend only on B_{\perp} , (e.g., electron-electron interactions) and therefore does not change upon an increase of B_T . The value of g in a tilted field can be calculated by the derivative of Δ_{ν} with respect to B_T , and it provides information about the spin of the excitation involved in the transport process [25]. The enhancement of g due to exchange interactions depends solely upon B_{\perp} and therefore does not influence the calculation. A linear fit to the data leads to $g \approx 2$ for the three filling factors at each B_{\perp} meaning that transport takes place via thermally excited electron-hole pairs with reversed spin with no collective effects, such as skyrmions [26], involved. To illustrate the behavior of g , we plot g as a function of ν at $B_{\perp} = 10.4$ and 11.3 T as representative results in Fig. 3(e).

In contrast to the even filling factors, the value of Δ_{-3} [Fig. 3(f)] does not depend on B_T and it is much smaller than the Zeeman energy. Therefore, we can assume that the origin of $\nu = -3$ lies in the lifting of the valley degeneracy in the $N = -1$ level.

We now turn our attention to $N = 0$, which, in a tilted magnetic field, behaves substantially different compared to the higher LLs. We first consider device A. Figure 4(a) shows that at $\nu = -1$ the minimum in R_{xx} becomes deeper, tilting the sample from $\theta = 0^\circ$ (black solid line) to $\theta = 59.1^\circ$ (red solid line) at $B_{\perp} = 14.1$ T. Accordingly, the gap associated with $\nu = -1$ increases with B_T [Fig. 4(b)]. The size of Δ_{-1} is larger than the Zeeman energy for $B_{\perp} \geq 20$ T, while it is compatible with E_Z within the error bars at smaller B_{\perp} . If a finite Landau level width is taken into account, then one can see that an enhancement of Δ_{-1} with respect to E_Z occurs also in the case of $B_{\perp} \leq 11.3$ T. Furthermore, as in the case of the even ν in $|N| > 0$, we do not find any significant enhancement of g from the dependence of Δ_{-1} on B_T [see the dotted line in Fig. 4(b)]. This indicates that $\nu = -1$ separates two states with reversed spin and the enhancement of the gap size, with respect to E_Z , is governed by the exchange interaction due to B_{\perp} .

At half filling of $N = 0$, the resistance maximum at $\nu = 0$ decreases with the in-plane magnetic field [see Fig. 4(c)] having $B_{\perp} \geq 2$ T, confirming earlier observations on suspended [16] and h-BN supported samples [15]. This observation suggests that Δ_0 is reduced upon increasing B_T , ruling out the scenario of a fully spin polarized state at half filled $N = 0$.

The capacitance measurements on device B in tilted magnetic fields support the picture emerging from the transport experiments. Figure 4(d) shows that all three ν resulting from the splitting of the zero energy Landau level react to a change in θ at a fixed $B_{\perp} = 10.1$ T. We also notice that the odd filling factors ± 1 are enhanced by an increase in B_T , i.e., the gap size increases, while the minimum at $\nu = 0$ becomes shallower as the sample

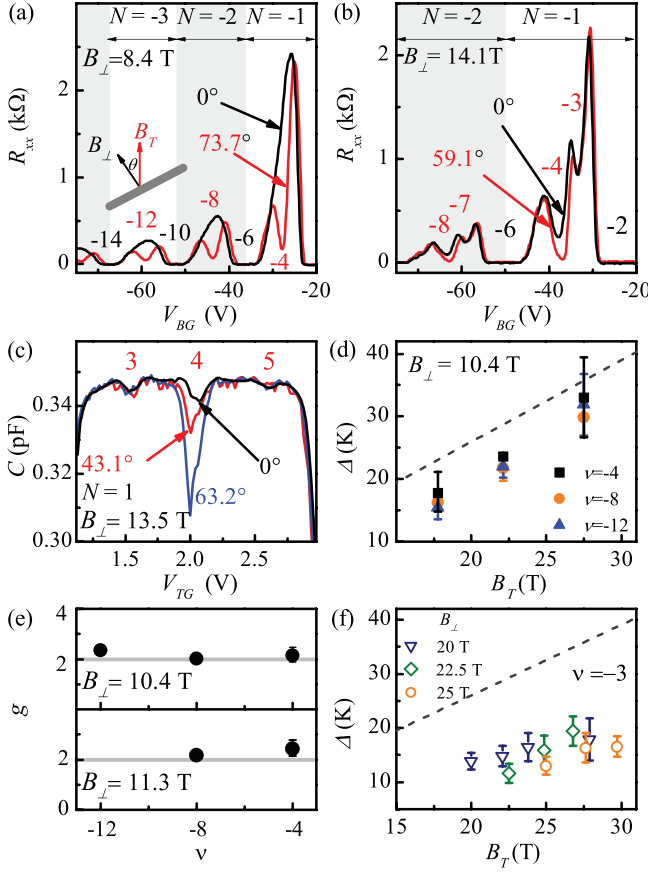


FIG. 3. (Color online) Splitting of the higher Landau levels in a tilted magnetic field at 1.4 K. (a) R_{xx} as a function of the back gate voltage at $B_{\perp} = 8.4$ T and $\theta = 0^{\circ}$ (black line) and at $\theta = 73.7^{\circ}$ (red line). Inset: Sketch of the tilting configuration. (b) R_{xx} for $N = -1$ and -2 at $B_{\perp} = 14.1$ T and $\theta = 0^{\circ}$ (black line) and $\theta = 59.1^{\circ}$ (red line). (c) Splitting of $N = 1$ observed in the capacitance signal at $B_{\perp} = 13.5$ T and $\theta = 0^{\circ}$ (black line), $\theta = 43.1^{\circ}$ (red line) and $\theta = 63.2^{\circ}$ (blue line). (d) Activation gaps for $\nu = -4$ (black squares), $\nu = -8$ (orange circles) and $\nu = -12$ (blue triangles) as a function of B_T at $B_{\perp} = 10.4$ T. The gray dashed line represents E_Z for $g = 2$. (e) g as a function of ν at $B_{\perp} = 10.4$ T (top panel) and 11.3 T (bottom panel). (f) Δ_{-3} as a function of B_T at $B_{\perp} = 20$ T (blue triangles), 22.5 T (green squares) and 25 T (orange circles).

is tilted from $\theta = 0^{\circ}$ (black solid line) and $\theta = 59.7^{\circ}$ (red solid line), i.e., the gap decreases.

The observation of the full splitting of the LLs in a perpendicular field and in particular, the presence of odd filling factors in $|N| \neq 0$, means that both samples show phenomenology typical of the quantum Hall ferromagnetism of graphene [3, 19]. In agreement with the QHF picture, we observe enhanced energy gaps in perpendicular field for both $\nu = -1$ and $\nu = -4$. In addition, the square root dependence of Δ_{-3} on B_{\perp} suggests that its origin is due to electron-electron interactions.

The tilted field experiments enable us to compose a splitting scenario which is different for the $N = 0$ level

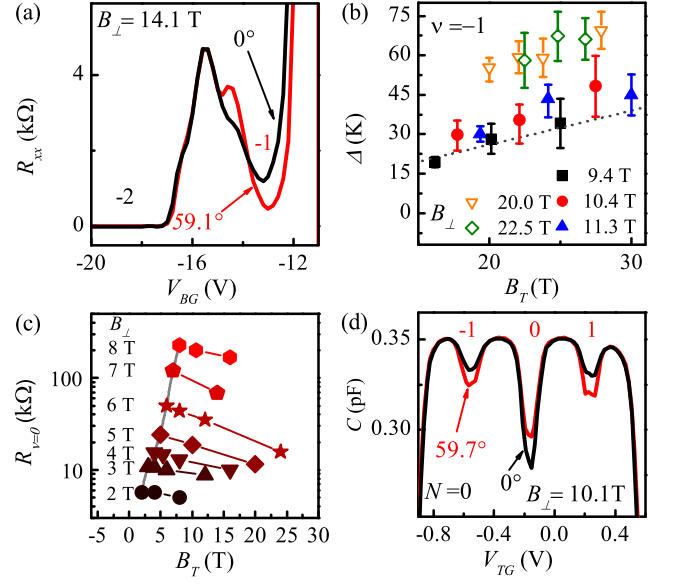


FIG. 4. (Color online) Splitting of $N = 0$ in a tilted magnetic field. (a) R_{xx} at $\nu = -1$ in $B_{\perp} = 14.1$ T and $\theta = 0^{\circ}$ (black line) and $\theta = 59.1^{\circ}$ (red line). (b) Activation gap for $\nu = -1$ as a function of B_T at different B_{\perp} ; the gray dotted line is E_Z calculated with $g = 2$. (c) Value of the resistance maximum at $\nu = 0$ in a tilted magnetic field as a function of B_T at different $9.4 \leq B_{\perp} \leq 22.5$ T and 4.2 K. (d) C at $B_{\perp} = 10.1$ T and $\theta = 0^{\circ}$ (black line) and $\theta = 59.7^{\circ}$ (red line).

and the higher energy levels. In the lowest level, we find that the spin and the valley degeneracy are lifted at $\nu = \pm 1$ and $\nu = 0$, respectively. Conversely, we find that for $N \neq 0$ the spin degeneracy is lifted at half filling while the valley degeneracy is lifted at quarter filling. It is worth pointing out the difference between $\nu = -1$ and the filling factors originating from the spin splitting in the higher levels: The size of Δ_{-1} cannot be explained solely by the Zeeman energy, but it must find an origin in the electron-electron interactions, whereas the gaps at $\nu = -4, -8$ and -12 appear to be Zeeman dominated.

In conclusion, we have probed the lifting of the Landau level degeneracy of graphene with two different measurement techniques and we have measured the activated transport gap for most of the observed filling factors. Our experiments in tilted fields highlight the differences between $N = 0$ and the higher energy levels, and we could probe the different splitting hierarchies in $N = \pm 1$ and $N = 0$, confirming the findings of Ref.15. However, probably due to the disorder in our sample, we did not find any indication for skyrmion excitations in the transport properties.

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